

Sets & Steps

Math Practice & Worked Solutions

Algebra 1

Perfect Squares, Vertex Form & Quadratic Formula | Algebra 1 | 4-Topic Bundle

4-topic bundle | 384 problems | Four activity formats

01 Special Binomial Products

View individual product and its full preview

02 Converting Quadratics to Vertex Form

View individual product and its full preview

03 Solving Quadratics by Completing the Square

View individual product and its full preview

04 Quadratic Formula

View individual product and its full preview

In every topic

Answer Bank Challenge	24 tasks
Grid Rounds	24 tasks
Match & Move	24 cards
Error Analysis & Strategy	24 tasks
Quick Answer Key and Full Worked Solutions	included
Teacher / Parent Use Guide and Terms of Use	included

Product previews

The following preview pages show the cover, all four activity formats, and worked examples for each included resource, in the listed order.

32 PDFs and 4 READMEs; 226 buyer PDF pages across the 4 products.

Preview pages are not included in the buyer page count. Check the list against resources you already own.

This is a fixed collection of the listed products. Purchase includes the existing individual resource files. To open a product's online preview, follow its title link and select View Preview.

Published by Tusils LLC.

Algebra 1
Special Binomial Products

Special Binomial Products | A1-U08-P06

96 problems · Four activity formats

01	Answer Bank Challenge	24 tasks
02	Grid Rounds	24 tasks
03	Match & Move	24 cards
04	Error Analysis & Strategy	24 tasks
05	Quick Answer Key	96 answers
06	Full Worked Solutions	96 solutions
07	Teacher / Parent Use Guide	included
08	Terms of Use & License	included

Topic focus
This topic is a focused set of 96 practice tasks on Special Binomial Products.
8 PDFs and a README; 50 buyer pages.

Algebra 1

Special Binomial Products

Name: _____ Date: _____ Class: _____

Answer each question and record the matching bank letter. Give exact values. A value without its unit is not a complete answer.

Determine the square when both degree-three monomial terms are negative. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(-2a^2b - 3bc^2)^2$ _____ Bank label: _____	Square each bivariate monomial and calculate their cross term. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(m^2n + 2mn^2)^2$ _____ Bank label: _____
Square the two full monomial terms and combine their exponents correctly. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(2p^2q - 5pq^2)^2$ _____ Bank label: _____	Expand the square of the bilinear monomial and constant. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(4mn + 5)^2$ _____ Bank label: _____
Turn the given square into a collected polynomial. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(7a^2b - 2)^2$ _____ Bank label: _____	Expand without factoring away the requested square structure. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(5uv^2 + 2u^2)^2$ _____ Bank label: _____
Expand the square before distributing the negative outer multiplier. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $-2(2y + 3)^2$ _____ Bank label: _____	Treat $y - 2$ as the second whole term, apply the square identity, and then remove the remaining parentheses. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(x + (y - 2))^2$ _____ Bank label: _____

Algebra 1

Special Binomial Products

Name: _____ Date: _____ Class: _____

Answer each question and show your reasoning in the workspace. Give exact values rather than decimals unless the question supplies a decimal. A value without its unit is not a complete answer.

Expand the square and verify that every resulting term has the same total degree. Expression: $(x^2 + 2xy)^2$ _____ _____	Give the exact product of the fractional conjugates. Expression: $((\frac{1}{2})x + 4)((\frac{1}{2})x - 4)$ _____ _____
Simplify the product with rational leading coefficient. Expression: $((\frac{2}{3})y - 3)((\frac{2}{3})y + 3)$ _____ _____	Treat ab as the common monomial and calculate the product. Expression: $(ab + 5)(ab - 5)$ _____ _____
Find the two monomials that survive this three-variable product. Expression: $(2xy - 3z)(2xy + 3z)$ _____ _____	Apply the identity to the two full bivariate monomials. Expression: $(m^2n + 2mn^2)(m^2n - 2mn^2)$ _____ _____

Algebra 1

Special Binomial Products

Name: _____ Date: _____ Class: _____

Begin at START. Answer the card, then find the matching final answer at the top of another card. Use the recording sheet for your reasoning. Visit each card once and continue to FINISH.

Incoming: $9y^4 - 6y^2z^3 + z^6$. Find the exact difference of monomial squares in this product. Expression: $(a^2b^3 + bc)(a^2b^3 - bc)$ Your response: _____	START Expand the square and include its doubled cross term. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(x + 3)^2$ Your response: _____
Incoming: $x^2 + 6x + 9$. Write this squared difference as a trinomial. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(y - 5)^2$ Your response: _____	Incoming: $25a^2 + 10ab + b^2$. Convert the square into a homogeneous quadratic in m and n. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(2m - 7n)^2$ Your response: _____
Incoming: $m^2 + 8mn + 16n^2$. Find the exact coefficients in the bivariate trinomial. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $((\frac{1}{4})x - 2y)^2$ Your response: _____	Incoming: $36a^2 + 4ab + (\frac{1}{9})b^2$. Expand and order the result by descending degree in x. Use the complete expanded polynomial as the matching response and retain the original identity explanation, including any cross term or cancellation. Expression: $(2 - x^2)^2$ Your response: _____

Algebra 1**Special Binomial Products****Name:** _____ **Date:** _____ **Class:** _____

Evaluate the supplied statement or method. Say whether it is correct, repair it if it is not, and verify the result exactly. Not every prompt contains an error.

Which listed method matches the expression's factor structure?

Expression: $(z + 8)^2$

binomial square

conjugate product

general distribution

Select the special-product pattern shown by these factors.

Expression: $(w + 10)(w - 10)$

binomial square

conjugate product

general distribution

Decide whether a special identity applies or ordinary distribution is required.

Expression: $(a + 2)(a + 5)$

binomial square

conjugate product

general distribution

Explain whether the opposite-looking constants justify a conjugate shortcut.

Expression: $(x + 5)(x - 4)$

Special Binomial Products

Full Worked Solutions - excerpt

Worked example

Problem. Find the exact difference of monomial squares in this product.

Expression: $(a^2b^3 + bc)(a^2b^3 - bc)$

Answer. $a^4b^6 - b^2c^2$.

Explanation and check.

Squaring the common term gives a^4b^6 and squaring the opposite term gives b^2c^2 .

Worked example

Problem. Explain whether the opposite-looking constants justify a conjugate shortcut.

Expression: $(x + 5)(x - 4)$

Answer. No; use general distribution.

Explanation and check.

Conjugates require exactly $+V$ and $-V$. Here $+5$ and -4 have different magnitudes, so their cross terms do not cancel.

Algebra 1
Converting Quadratics to Vertex Form

Converting Quadratics to Vertex Form | A1-U09-P04

96 problems · Four activity formats

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Topic focus
This topic is a focused set of 96 practice tasks on Converting Quadratics to Vertex Form.
8 PDFs and a README; 56 buyer pages.

Algebra 1

Converting Quadratics to Vertex Form

Name: _____ Date: _____ Class: _____

Answer each question and record the matching bank letter. Give exact values. Give the whole requested response, including any reasoning the question asks for.

Complete the inner square and scale its compensation. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="154 604 795 640"> <tr> <td>Standard</td> <td>$3x^2 + 18x + 20$</td> </tr> </table> _____ Bank label: _____	Standard	$3x^2 + 18x + 20$	Convert the downward-opening quadratic. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="826 604 1468 640"> <tr> <td>Standard</td> <td>$-3x^2 + 24x + 1$</td> </tr> </table> _____ Bank label: _____	Standard	$-3x^2 + 24x + 1$
Standard	$3x^2 + 18x + 20$				
Standard	$-3x^2 + 24x + 1$				
Express the scaled perfect square in vertex form. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="154 940 795 976"> <tr> <td>Standard</td> <td>$4x^2 - 24x + 36$</td> </tr> </table> _____ Bank label: _____	Standard	$4x^2 - 24x + 36$	Rewrite without a trailing zero constant. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="826 940 1468 976"> <tr> <td>Standard</td> <td>$-4x^2 - 16x - 16$</td> </tr> </table> _____ Bank label: _____	Standard	$-4x^2 - 16x - 16$
Standard	$4x^2 - 24x + 36$				
Standard	$-4x^2 - 16x - 16$				
Convert and retain the remainder after the scaled square. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="154 1276 795 1312"> <tr> <td>Standard</td> <td>$6x^2 - 12x + 8$</td> </tr> </table> _____ Bank label: _____	Standard	$6x^2 - 12x + 8$	Rewrite to reveal the left-shifted vertex. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="826 1276 1468 1312"> <tr> <td>Standard</td> <td>$-6x^2 - 36x - 50$</td> </tr> </table> _____ Bank label: _____	Standard	$-6x^2 - 36x - 50$
Standard	$6x^2 - 12x + 8$				
Standard	$-6x^2 - 36x - 50$				
Convert and compute the scaled correction. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="154 1612 795 1648"> <tr> <td>Standard</td> <td>$7x^2 + 28x + 19$</td> </tr> </table> _____ Bank label: _____	Standard	$7x^2 + 28x + 19$	Write the exact vertex form. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="826 1577 1468 1612"> <tr> <td>Standard</td> <td>$-7x^2 + 28x - 11$</td> </tr> </table> _____ Bank label: _____	Standard	$-7x^2 + 28x - 11$
Standard	$7x^2 + 28x + 19$				
Standard	$-7x^2 + 28x - 11$				

Algebra 1

Converting Quadratics to Vertex Form

Name: _____ Date: _____ Class: _____

Answer each question and show your reasoning in the workspace. Give exact values rather than decimals unless the question supplies a decimal. Give the whole requested response, including any reasoning the question asks for.

Fill both equal blanks.

Trace

$$x^2 + 4x + 9 = (x^2 + 4x + \underline{\hspace{1cm}} - \underline{\hspace{1cm}}) + 9 = (x + 2)^2 + 5$$

What number belongs in both blanks?

Trace

$$x^2 - 6x + 1 = (x^2 - 6x + \underline{\hspace{1cm}}) - \underline{\hspace{1cm}} + 1 = (x - 3)^2 - 8$$

Algebra 1

Converting Quadratics to Vertex Form

Name: _____ Date: _____ Class: _____

Begin at START. Answer the card, then find the matching final answer at the top of another card. Use the recording sheet for your reasoning. Visit each card once and continue to FINISH.

Incoming: $(x + \frac{7}{2})^2 - \frac{69}{4}$ Complete the square for $x^2 + x$. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="151 632 797 663"> <tr> <td>Standard</td> <td>$x^2 + x$</td> </tr> </table> Your response: _____	Standard	$x^2 + x$	Incoming: $(x + 12)^2 - 1$ Extract the completed square from the trinomial. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="828 648 1471 680"> <tr> <td>Standard</td> <td>$x^2 - 24x + 160$</td> </tr> </table> Your response: _____	Standard	$x^2 - 24x + 160$
Standard	$x^2 + x$				
Standard	$x^2 - 24x + 160$				
Incoming: $(x - \frac{9}{2})^2 - \frac{81}{4}$ Rewrite using a single rational vertical offset. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="151 1087 797 1119"> <tr> <td>Standard</td> <td>$x^2 + 7x - 5$</td> </tr> </table> Your response: _____	Standard	$x^2 + 7x - 5$	Incoming: $(x + \frac{11}{2})^2 - \frac{41}{4}$ Convert and include an exact form that expands back to 50 as the constant. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="828 1087 1471 1119"> <tr> <td>Standard</td> <td>$x^2 + 15x + 50$</td> </tr> </table> Your response: _____	Standard	$x^2 + 15x + 50$
Standard	$x^2 + 7x - 5$				
Standard	$x^2 + 15x + 50$				
Incoming: $(x - 11)^2 + 1$ Write vertex form and show the one-unit deficit. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="151 1509 797 1541"> <tr> <td>Standard</td> <td>$x^2 + 24x + 143$</td> </tr> </table> Your response: _____	Standard	$x^2 + 24x + 143$	Incoming: $(x + \frac{1}{2})^2 - \frac{1}{4}$ Rewrite and keep all constants as fractions. Match the complete requested vertex form. Preserve the outside coefficient and compensating constant; the expanded standard form alone is not the requested response. <table border="1" data-bbox="828 1518 1471 1549"> <tr> <td>Standard</td> <td>$x^2 - x + 6$</td> </tr> </table> Your response: _____	Standard	$x^2 - x + 6$
Standard	$x^2 + 24x + 143$				
Standard	$x^2 - x + 6$				

Algebra 1

Converting Quadratics to Vertex Form

Name: _____ Date: _____ Class: _____

Evaluate the supplied statement or method. Say whether it is correct, repair it if it is not, and verify the result exactly. Not every prompt contains an error.

Rewrite the quadratic in vertex form. Choose how to organize the conversion: insert and compensate a square-completing term, or compare coefficients with a squared-binomial form. Explain which route suits the coefficients, then give the original requested vertex form and verify it.

Standard	$x^2 + 6x + 5$
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Complete the square and state the equivalent vertex form. Choose how to organize the conversion: insert and compensate a square-completing term, or compare coefficients with a squared-binomial form. Explain which route suits the coefficients, then give the original requested vertex form and verify it.

Standard	$x^2 - 8x + 19$
----------	-----------------

Put $x^2 + 10x$ into vertex form without changing its values. Choose how to organize the conversion: insert and compensate a square-completing term, or compare coefficients with a squared-binomial form. Explain which route suits the coefficients, then give the original requested vertex form and verify it.

Standard	$x^2 + 10x$
----------	-------------

Find the vertex form and identify the final constant. Choose how to organize the conversion: insert and compensate a square-completing term, or compare coefficients with a squared-binomial form. Explain which route suits the coefficients, then give the original requested vertex form and verify it.

Standard	$x^2 - 4x - 12$
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Converting Quadratics to Vertex Form

Full Worked Solutions - excerpt

Worked example

Problem. Complete the final equality.

Trace	$x^2 + 8x + 3 = (x + 4)^2 - 16 + 3 = (x + 4)^2 + \underline{\hspace{2cm}}$
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Answer. -13

Explanation and check.

Combine -16 and 3 .

Worked example

Problem. Use the last equality to recover the original constant c .

Trace	$4x^2 - 16x + c = 4[(x - 2)^2 - 4] + c = 4(x - 2)^2 + 9$
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Answer. 25

Explanation and check.

The final constant is $c - 16$, so $c - 16 = 9$.

Algebra 1
Solving Quadratics by Completing the Square

Solving Quadratics by Completing the Square | A1-U09-P09

96 problems · Four activity formats

01	Answer Bank Challenge	24 tasks
02	Grid Rounds	24 tasks
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Topic focus
This topic is a focused set of 96 practice tasks on Solving Quadratics by Completing the Square.
8 PDFs and a README; 62 buyer pages.

Algebra 1

Solving Quadratics by
Completing the Square

Name: _____ Date: _____ Class: _____

Answer each question and record the matching bank letter. Give exact values. A value without its unit is not a complete answer.

Complete the square and solve the symmetric integer branches. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 + 16x + 60 = 0$. _____ Bank label: _____	Find the center and both roots using equality-preserving additions. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 - 14x + 40 = 0$. _____ Bank label: _____
Preserve the exact nonsquare distance from the completed center. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 + 18x + 70 = 0$. _____ Bank label: _____	Complete the square with a negative linear term. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 - 2x - 10 = 0$. _____ Bank label: _____
Build the square and simplify the exact solution statement. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 + 12x + 29 = 0$. _____ Bank label: _____	Use the fractional half-coefficient and give exact roots. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 + 3x - 1 = 0$. _____ Bank label: _____
Complete the square without rounding the half-integer center. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 - 5x + 2 = 0$. _____ Bank label: _____	Track the quarter fractions created by the odd coefficient. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 + 7x + 3 = 0$. _____ Bank label: _____

Algebra 1

Solving Quadratics by
Completing the Square

Name: _____ Date: _____ Class: _____

Answer each question and show your reasoning in the workspace. Give exact values rather than decimals unless the question supplies a decimal. A value without its unit is not a complete answer.

Supply the omitted line and finish the partial solution. Work over the real numbers with $x^2 + 6x = 7$. $x^2 + 6x = 7$ _____ $(x + 3)^2 = 16$ _____ _____	Fill the equality-preserving completion step. Work over the real numbers with $x^2 - 8x = -7$. $x^2 - 8x = -7$ _____ $(x - 4)^2 = 9$ _____ _____
Supply the normalization line that must precede square completion. Work over the real numbers with $2x^2 + 12x = 10$. $2x^2 + 12x = 10$ _____ $x^2 + 6x + 9 = 5 + 9$ _____ _____	Repair the trace by supplying the omitted signed branch. Work over the real numbers with $x^2 + 4x - 5 = 0$. $(x + 2)^2 = 9$ $x + 2 = 3$ $x = 1$ _____ _____
Determine the fractional amount missing from both sides. Work over the real numbers with $x^2 + 5x = 2$. $x^2 + 5x = 2$ $x^2 + 5x + \underline{\hspace{1cm}} = 2 + \underline{\hspace{1cm}}$ _____ _____	Replace the trinomial with its equivalent squared-binomial form. Work over the real numbers with $x^2 - 6x + 9 = 14$. $x^2 - 6x + 9 = 14$ _____ $x - 3 = \pm\sqrt{14}$ _____ _____

Algebra 1

Solving Quadratics by
Completing the Square

Name: _____ Date: _____ Class: _____

Begin at START. Answer the card, then find the matching final answer at the top of another card. Use the recording sheet for your reasoning. Visit each card once and continue to FINISH.

Incoming: amount added to each side: $\frac{25}{16}$; completed square equation: $(x - \frac{5}{4})^2 = \frac{31}{16}$; real solution count: 2; solutions: $\frac{5-\sqrt{31}}{4}, \frac{5+\sqrt{31}}{4}$; square root radicand: $\frac{31}{16}$ Recognize the repeated root created by a rational completion amount. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 + (\frac{7}{5})x + \frac{49}{100} = 0$. Your response: _____	Incoming: amount added to each side: $\frac{9}{16}$; completed square equation: $(x + \frac{3}{4})^2 = \frac{33}{16}$; real solution count: 2; solutions: $\frac{-3-\sqrt{33}}{4}, \frac{-3+\sqrt{33}}{4}$; square root radicand: $\frac{33}{16}$ Normalize the leading coefficient before completing the square. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $2x^2 + 8x + 1 = 0$. Your response: _____
Incoming: amount added after normalizing: 1; completed square equation: $(x - 1)^2 = \frac{8}{5}$; leading coefficient divisor: 5; normalized equation: $x^2 - 2x - \frac{3}{5} = 0$; real solution count: 2; solutions: $1 - 2 \cdot \frac{\sqrt{10}}{5}, 1 + 2 \cdot \frac{\sqrt{10}}{5}$; square root radicand: $\frac{8}{5}$ Use normalization to expose the repeated root. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $2x^2 - 4x + 2 = 0$. Your response: _____	Incoming: amount added after normalizing: $\frac{25}{4}$; completed square equation: $(x - \frac{5}{2})^2 = \frac{13}{12}$; leading coefficient divisor: 6; normalized equation: $x^2 - 5x + \frac{31}{6} = 0$; real solution count: 2; solutions: $\frac{5}{2} - \frac{\sqrt{39}}{6}, \frac{5}{2} + \frac{\sqrt{39}}{6}$; square root radicand: $\frac{13}{12}$ Normalize the odd linear coefficient and solve exactly. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $4x^2 + 20x + 11 = 0$. Your response: _____
Incoming: amount added after normalizing: $\frac{9}{4}$; completed square equation: $(x + \frac{3}{2})^2 = \frac{1}{4}$; leading coefficient divisor: 10; normalized equation: $x^2 + 3x + 2 = 0$; real solution count: 2; solutions: $-2, -1$; square root radicand: $\frac{1}{4}$ Normalize and simplify the small exact radius. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $12x^2 - 24x + 11 = 0$. Your response: _____	START Rearrange the constants and use the completed-square sign to classify roots. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals. Work over the real numbers with $x^2 - 5x + 9 = 2$. Your response: _____

Algebra 1

Solving Quadratics by Completing the Square

Name: _____ Date: _____ Class: _____

Evaluate the supplied statement or method. Say whether it is correct, repair it if it is not, and verify the result exactly. Not every prompt contains an error.

Complete the square and keep both exact radical branches. Choose between adding the completing quantity to both sides and inserting a compensating pair on the left before isolating the square. Justify the clearer equality-preserving route, then solve by the requested square completion.

Work over the real numbers with $x^2 + 6x + 1 = 0$.

Use half the linear coefficient to build the square. Choose between adding the completing quantity to both sides and inserting a compensating pair on the left before isolating the square. Justify the clearer equality-preserving route, then solve by the requested square completion.

Work over the real numbers with $x^2 - 4x - 3 = 0$.

Show the equal addition that creates a perfect-square trinomial. Choose between adding the completing quantity to both sides and inserting a compensating pair on the left before isolating the square. Justify the clearer equality-preserving route, then solve by the requested square completion.

Work over the real numbers with $x^2 + 8x + 5 = 0$.

Complete the square and simplify the resulting radical. Choose between adding the completing quantity to both sides and inserting a compensating pair on the left before isolating the square. Justify the clearer equality-preserving route, then solve by the requested square completion.

Work over the real numbers with $x^2 - 10x + 7 = 0$.

Solving Quadratics by Completing the Square

Full Worked Solutions - excerpt

Worked example

Problem. Use normalization to expose the repeated root. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals.

Work over the real numbers with $2x^2 - 4x + 2 = 0$.

Answer. amount added after normalizing: 1; completed square equation: $(x - 1)^2 = 0$; leading coefficient divisor: 2; normalized equation: $x^2 - 2x + 1 = 0$; real solution count: 1; solutions: 1; square root radicand: 0

Explanation and check.

Dividing by 2 already displays the perfect square $x^2 - 2x + 1$. Its only root is $x = 1$.

Worked example

Problem. Show how negative normalization reveals a zero radius. Match the complete exact real solution set and show every originally requested square isolation, equality-preserving step, and branch. Do not replace exact radicals with decimals.

Work over the real numbers with $-5x^2 + 20x - 20 = 0$.

Answer. amount added after normalizing: 4; completed square equation: $(x - 2)^2 = 0$; leading coefficient divisor: -5; normalized equation: $x^2 - 4x + 4 = 0$; real solution count: 1; solutions: 2; square root radicand: 0

Explanation and check.

Every term divided by -5 gives the perfect square $x^2 - 4x + 4$. Hence $x = 2$ is repeated.

Algebra 1
Quadratic Formula

Quadratic Formula | A1-U09-P10
96 problems · Four activity formats

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Topic focus
This topic is a focused set of 96 practice tasks on Quadratic Formula.
8 PDFs and a README; 58 buyer pages.

Algebra 1

Quadratic Formula

Name: _____ Date: _____ Class: _____

Answer each question and record the matching bank letter. Give exact values. Give the whole requested response, including any reasoning the question asks for.

Consider $4x^2 + 9 = 12x$ over the real numbers. Rewrite with zero on one side and identify the coefficient used for $-b$. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. _____ Bank label: _____	Consider $x(x - 3) = 10$ over the real numbers. Expand the product and normalize before filling the formula slots. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. _____ Bank label: _____
Consider $2x(x + 4) = 3$ over the real numbers. Distribute the outside factors and determine the signed constant after normalization. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. _____ Bank label: _____	Consider $(x - 2)(x + 5) = 7$ over the real numbers. Expand, combine the product constant with the right-side value, and then identify coefficients. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. _____ Bank label: _____
Consider $3(x^2 - 2) = x + 1$ over the real numbers. Remove grouping and collect both right-side terms before entering a, b, and c. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. _____ Bank label: _____	Consider $(x + 1)^2 = 8$ over the real numbers. Convert the square to standard zero form for a formula substitution. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. _____ Bank label: _____
Consider $5x^2 = 2(x + 3)$ over the real numbers. Distribute the right side and move its two terms with the correct signs. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. _____ Bank label: _____	Consider $0.5x^2 - 1.5x = 2$ over the real numbers. Keep the fractional coefficients rather than clearing them, and normalize c correctly. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. _____ Bank label: _____

Algebra 1

Quadratic Formula

Name: _____ Date: _____ Class: _____

Answer each question and show your reasoning in the workspace. Give exact values rather than decimals unless the question supplies a decimal. Give the whole requested response, including any reasoning the question asks for.

Consider $6x - 5 = 2x^2$ over the real numbers. Place the quadratic term first without losing the signs of the other terms. _____ _____	Consider $4 - x(x + 2) = 0$ over the real numbers. Use an equivalent positive-leading normalization and state the coefficient triple it creates. _____ _____												
Consider $-(x - 4)^2 = 3x - 20$ over the real numbers. Expand the leading negative square, collect, and choose a positive-leading zero form. _____ _____	Consider $x^2 + x - 1 = 0$ over the real numbers. Round the final approximations to 2 decimal places. Report the exact pair first and then fill a hundredths-and-residual table. <table border="1" style="width: 100%; border-collapse: collapse; margin-bottom: 10px;"> <thead> <tr> <th style="padding: 5px;">branch</th> <th style="padding: 5px;">exact root</th> <th style="padding: 5px;">rounded to 2 places</th> <th style="padding: 5px;">absolute residual</th> </tr> </thead> <tbody> <tr> <td style="padding: 5px;">Smaller root</td> <td style="padding: 5px;">_____</td> <td style="padding: 5px;">_____</td> <td style="padding: 5px;">_____</td> </tr> <tr> <td style="padding: 5px;">Larger root</td> <td style="padding: 5px;">_____</td> <td style="padding: 5px;">_____</td> <td style="padding: 5px;">_____</td> </tr> </tbody> </table> _____ _____	branch	exact root	rounded to 2 places	absolute residual	Smaller root	_____	_____	_____	Larger root	_____	_____	_____
branch	exact root	rounded to 2 places	absolute residual										
Smaller root	_____	_____	_____										
Larger root	_____	_____	_____										
Consider $2x^2 - x - 2 = 0$ over the real numbers. Round the final approximations to 2 decimal places. Approximate each branch to the nearest hundredth and substitute the rounded results. <table border="1" style="width: 100%; border-collapse: collapse; margin-bottom: 10px;"> <thead> <tr> <th style="padding: 5px;">branch</th> <th style="padding: 5px;">exact root</th> <th style="padding: 5px;">rounded to 2 places</th> <th style="padding: 5px;">absolute residual</th> </tr> </thead> <tbody> <tr> <td style="padding: 5px;">Smaller root</td> <td style="padding: 5px;">_____</td> <td style="padding: 5px;">_____</td> <td style="padding: 5px;">_____</td> </tr> <tr> <td style="padding: 5px;">Larger root</td> <td style="padding: 5px;">_____</td> <td style="padding: 5px;">_____</td> <td style="padding: 5px;">_____</td> </tr> </tbody> </table> _____ _____	branch	exact root	rounded to 2 places	absolute residual	Smaller root	_____	_____	_____	Larger root	_____	_____	_____	Consider $3x^2 - 2x - 2 = 0$ over the real numbers. Round the final approximations to 2 decimal places. Simplify the exact radical before giving hundredth approximations. _____ _____
branch	exact root	rounded to 2 places	absolute residual										
Smaller root	_____	_____	_____										
Larger root	_____	_____	_____										

Algebra 1

Quadratic Formula

Name: _____ Date: _____ Class: _____

Begin at START. Answer the card, then find the matching final answer at the top of another card. Use the recording sheet for your reasoning. Visit each card once and continue to FINISH.

START Consider $8x^2 + 2x - 3 = 0$ over the real numbers. Evaluate the radical 10 and reduce the two sixteenth-denominator branches. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. Your response: _____	Incoming: $\{1, \frac{7}{2}\}$ Consider $3x^2 - 5x = 2x^2 + 6$ over the real numbers. Collect the quadratic terms first and apply the formula to the net leading coefficient. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. Your response: _____
Incoming: $\{1\}$ Consider $16x^2 + 24x + 9 = 0$ over the real numbers. Evaluate the formula at a zero discriminant with an even denominator reduction. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. Your response: _____	Incoming: $\{-1, \frac{7}{2}\}$ Consider $(3x - 2)^2 = 25$ over the real numbers. Expand the affine square and solve the resulting quadratic by the complete formula. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. Your response: _____
Incoming: $\{-2 - \sqrt{3}, -2 + \sqrt{3}\}$ Consider $2x^2 - 3x - 1 = 0$ over the real numbers. State the exact formula roots when the positive discriminant has no square factor. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. Your response: _____	Incoming: $\{-2, 3\}$ Consider $3x^2 - 12 = 0$ over the real numbers. Use $a = 3$ and $b = 0$ directly rather than simplifying the equation first. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set. Your response: _____

Algebra 1

Quadratic Formula

Name: _____ Date: _____ Class: _____

Evaluate the supplied statement or method. Say whether it is correct, repair it if it is not, and verify the result exactly. Not every prompt contains an error.

Consider $2x^2 + 3x - 5 = 0$ over the real numbers. Read a , b , and c with their signs, then write the full quadratic-formula substitution. Choose how to organize the arithmetic: calculate the discriminant first and then insert it, or write the complete signed formula substitution before simplifying any component. Justify your choice for these coefficients, then show the coefficients and the full formula substitution.

Consider $4x^2 - 9 = 0$ over the real numbers. Insert the absent term explicitly before setting up the formula. Choose how to organize the arithmetic: calculate the discriminant first and then insert it, or write the complete signed formula substitution before simplifying any component. Justify your choice for these coefficients, then show the coefficients and the full formula substitution.

Consider $-x^2 + 6x + 7 = 0$ over the real numbers. Keep the displayed leading sign and form the denominator $2a$. Choose how to organize the arithmetic: calculate the discriminant first and then insert it, or write the complete signed formula substitution before simplifying any component. Justify your choice for these coefficients, then show the coefficients and the full formula substitution.

Consider $3x^2 - 8x + 2 = 0$ over the real numbers. Record the coefficient triple and the unsimplified radical expression. Choose how to organize the arithmetic: calculate the discriminant first and then insert it, or write the complete signed formula substitution before simplifying any component. Justify your choice for these coefficients, then show the coefficients and the full formula substitution.

Quadratic Formula

Full Worked Solutions - excerpt

Worked example

Problem. Consider $6x - 5 = 2x^2$ over the real numbers. Place the quadratic term first without losing the signs of the other terms.

Answer. coefficients: $a: 2; b: -6; c: 5$; discriminant: -4 ; formula substitution: $x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(2)(5)}}{2(2)}$; normalized equation: $2x^2 - 6x + 5 = 0$; solutions:

Explanation and check.

Subtracting the left side from both sides gives $2x^2 - 6x + 5 = 0$, so $a = 2, b = -6, c = 5$.

Worked example

Problem. Consider $(x + 1)^2 = 8$ over the real numbers. Convert the square to standard zero form for a formula substitution. Use the quadratic formula, show your substitution and simplification, and match the complete exact real solution set.

Answer. $\{-1 + 2 \cdot \sqrt{2}, -2 \cdot \sqrt{2} - 1\}$

Explanation and check.

The signed coefficients are $a = 1, b = 2, c = -7$. In standard form, $x^2 + 2x - 7 = 0$. The discriminant is 32. Substitution in the quadratic formula gives $x = \frac{-(2) \pm \sqrt{(2)^2 - 4(1)(-7)}}{2(1)}$. Expanding gives $x^2 + 2x + 1 = 8$; moving 8 left gives $c = -7$ while $b = 2$.